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# Local Unfolding of Cu, Zn Superoxide Dismutase Monomer Determines the Morphology of

### **Fibrillar Aggregates**

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49 50 amyotrophic lateral sclerosis patients. The fibrillar aggregates formed by wild type and various disease-associated mutants have recently been found to have distinct cores and morphologies. Previous computational and experimental studies of wild-type SOD1 suggest that the apo-monomer, highly aggregation prone, displays substantial local unfolding dynamics. The residual folded structure of locally unfolded apoSOD1 corresponds to peptide segments forming the aggregation core as identified by a combination of proteolysis and mass spectroscopy. Therefore, we hypothesize that the destabilization of apoSOD1 caused by various mutations leads to distinct local unfolding dynamics. The partially unfolded structure, exposing the hydrophobic core and backbone hydrogen bond donors and acceptors, is prone to aggregate. The peptide segments in the residual folded structures form the "building block" for aggregation, which in turn determines the morphology of the aggregates. To test this hypothesis, we apply a multiscale simulation approach to study the aggregation of three typical SOD1 variants: wild type, G37R, and I149T. Each of these SOD1 variants has distinct peptide segments forming the core structure and features different aggregate morphologies. We perform atomistic molecular dynamics simulations to study the conformational dynamics of apoSOD1 monomer and coarse-grained molecular dynamics simulations to study the aggregation of partially unfolded SOD1 monomers. Our computational studies of monomer local unfolding and the aggregation of different SOD1 variants are consistent with experiments, supporting the hypothesis of the formation of aggregation "building blocks" via apo-monomer local unfolding as the mechanism of SOD1 fibrillar aggregation.

Aggregation of Cu, Zn superoxide dismutase (SOD1) is often found in

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#### Introduction

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\*Corresponding author. E-mail address: dokh@unc.edu. Abbreviations used: SOD1, superoxide dismutase; ALS, amyotrophic lateral sclerosis; DMD, discrete molecular dynamics; WHAM, weighted histogram analysis method; RMSF, root-mean-square fluctuation. The misfolding and aggregation of Cu, Zn 53 superoxide dismutase (SOD1) is associated with 54 amyotrophic lateral sclerosis (ALS).<sup>1,2</sup> More than 55 100 mutations in SOD1 have been identified in 56 familial ALS patients. Both wild-type and mutant 57

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SOD1 can form insoluble fibrillar aggregates with a 58common cross- $\beta$  amyloid structure, <sup>3,4</sup> as observed 5960 in many other amyloidogenic proteins with distinct primary, secondary, and tertiary structures.<sup>5</sup> Many 61 of the research efforts in SOD1 misfolding have been 62 focused on finding a general mechanism for how 63 mutations promote SOD1 misfolding and aggrega-64 tion, under the assumption of a common "mutation-65independent" aggregation pathway and similar aggregate structures. However, a recent study of 66 67 SOD1 aggregates formed by wild type and various 68 mutants revealed distinct fibrillar core compositions 69 and aggregate morphologies.<sup>7</sup> Accordingly, pheno-70typic heterogeneity has been reported in familial 71 ALS patients with different SOD1 mutations.<sup>8</sup> 72Increasing evidence suggests that the structures 73 74 and morphologies of protein aggregates affect their respective disease phenotypes and that polymor-75phism in protein aggregates associates with pheno-typic heterogeneity.<sup>9–12</sup> Hence, uncovering the 76 77 molecular mechanism governing the formation of 78polymorphic amyloid aggregates is important for 79gaining an understanding of ALS phenotypic 80 heterogeneity. 81

SOD1 forms a stable dimer in solution, with each 82 SOD1 monomer binding one copper and one zinc 83 ion and forming one intra-monomer disulfide bond. 84 Various biochemical and biophysical studies have 85 86 suggested that wild-type SOD1 dimer is exception-87 ally stable because of the coordination of metal ions.<sup>13</sup> Mounting experimental and computational 88 evidence suggest that apoSOD1 monomer is the 89 most aggregation prone species.<sup>14–19</sup> The loss of the 90 coordinated metal ions destabilizes the protein with 91 a significant population unfolded at physiological 92conditions.<sup>14</sup> Although apoSOD1 is native like in the crystal structure,<sup>20</sup> the protein in solution 9394features significant structural disorder and confor-95 mational flexibility.<sup>21</sup> Both experimental<sup>22,23</sup> and 96 computational<sup>19</sup> studies suggest that the apoSOD1 97 monomer features frequent local unfolding. In 98 addition to the two long loops, the metal-coordi-99 nated (in the native state) strands 4, 5, and 7 feature 100a high level of local unfolding, and the N-terminal 101  $\beta$ -sheet is the most stable structural element (Fig. 1021a). Interestingly, the same regions that are stable in 103 the locally unfolded apoSOD1 also correspond to 104 those regions that participate in the fibrillar core of 105 wild-type SOD1 aggregates, having been identified 106 as proteolysis-resistant peptides.<sup>7</sup> This observation 107 is consistent with the generic aggregation mecha-108 nism proposed earlier,<sup>24,25</sup> where the residual 109structural elements in the partially unfolded protein 110 interact with each other and serve as "building 111 blocks" for the formation of fibrillar amyloid 112aggregates. Recently, local unfolding induced by 113114 mutations has also been found to play an important role in the aggregation of  $\gamma$ -crystallin in human 115cataracts.<sup>26</sup> Therefore, we hypothesize that the 116

various disease-causative mutations in SOD1 have 117 different impacts on apoSOD1 conformational 118 dynamics, which in turn lead to distinct patterns 119 of local unfolding and thus the varied morphol- 120 ogies of the resulted aggregates. 121

To test this hypothesis, we apply a multiscale 122 molecular dynamics approach to study the local 123 unfolding of SOD1 monomer and the aggregation 124 dynamics of multiple monomers. In the previous 125 experimental study of SOD1 aggregates, Furukawa 126 et al. discovered that three major regions comprise 127 the fibril aggregate cores, including the N-terminal 128  $\beta$ -sheet (strands 1–3), the middle strand 6, and the 129 C-terminal strand 8 (Fig. 1b). The N-terminal 130 strands are observed in the aggregates formed by 131 all SOD1 variants. As a result, there are only three 132 possible combinations of core-forming peptide 133 patterns: all three segments, the N-terminal sheet 134 plus the middle strand, and the N-terminal sheet 135 plus the C-terminal strand. Therefore, beside the 136 wild-type SOD1 whose aggregation core is com- 137 posed of all three segments, we also include two 138 mutants, G37R and I149T, having representative 139 aggregation core compositions.<sup>7</sup> In the core of 140 G37R and I149T, the C-terminal strand and the 141 middle strand 6 are observed, respectively, in 142 addition to the N-terminal strands (Fig. 1b). In 143 order to probe the monomer conformational 144 dynamics, we perform atomistic discrete molecular 145 dynamics (DMD) simulations.<sup>19</sup> In the atomistic 146 simulations, we find that different mutations 147 indeed result in different patterns of local unfold- 148 ing and that the residual structures in the locally 149 unfolded states are consistent with the core- 150 forming segments, supporting the "building 151 block" aggregation mechanism.<sup>24</sup> We further 152 perform coarse-grained DMD simulations to 153 study SOD1 monomer aggregation for each of 154 the three SOD1 variants. To promote the formation 155 of partially unfolded structures, we develop a 156 hybrid structure-based interaction model where 157 the interactions between the core-forming residues 158 are enhanced. The reconstructed model structure 159 of the amyloid aggregates is consistent with the 160 experimentally observed morphology. Therefore, 161 our multiscale simulations suggest a molecular 162 mechanism of mutation-dependent SOD1 aggrega- 163 tion polymorphism. 164

#### **Results and Discussion**

We use a multiscale molecular dynamics ap- 166 proach to study the misfolding and aggregation of 167 apoSOD1. We use the atomistic DMD simulations<sup>27</sup> 168 to sample the conformational dynamics of the 169 apoSOD1 monomer, the timescale of which is 170 approximately microseconds to milliseconds. For 171 monomer aggregation, which spans hours and days, 172

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Fig. 1. The thermodynamics of apoSOD1 monomer. (a) In SOD1 monomer, the two metal ions (spheres) are coordinated by residues (sticks) in strands 4, 5, and 7. The amyloid core of wild-type (WT) SOD1 is composed of the N-terminal strands 1–3 (blue to cyan), the middle strand 6 (yellow), and the C-terminal strand 8 (red). Other regions are colored gray. The two mutated residues in this study, G37 and I149, are shown in sphere. (b) The regions forming the amyloid core of three typical SOD1 variants: WT, G37R, and I149T. The arrows illustrate the strands along the primary sequence. The thick lines highlight the regions found in the proteolysis-resistant amyloid core for each of the three SOD1 variants. (c) The specific heat of the WT apoSOD1 as a function of temperature. The specific heat values and corresponding statistical uncertainties (shown as error bars) are computed using WHAM analysis of the replica exchange simulation trajectories (Materials and Methods). At temperatures below the low-temperature peak, the protein is native like with the  $\beta$ -barrel intact. At temperatures higher than the high-temperature peak, the protein is unfolded, without persistent secondary and tertiary structures. At the intermediate temperature between the two peaks, the protein is partially unfolded. (d) The specific heat curves for all three variants feature similar local unfolding and global unfolding thermodynamics.

we use coarse-grained DMD simulations<sup>24</sup> with experimental constraints to enhance sampling of protein aggregation.

## 176 Conformational dynamics of apoSOD1177 monomer

We perform all-atom DMD simulations<sup>27</sup> to sample the conformational dynamics of apoSOD1 monomers. The protein is in united-atom representation, with all heavy atoms and polar hydrogen 181 explicitly modeled. The simulation is performed 182 with implicit solvent, and interatomic interactions 183 are modeled by a physical force field adapted from 184 Medusa, <sup>28</sup> which includes van der Waals, 185 solvation, <sup>29</sup> and hydrogen bonding potentials. In 186 addition to the previous version of the all-atom DMD 187 force field, <sup>27</sup> we also introduce screened electrostatic 188 interactions between charged residues (Materials 189 and Methods). Atomistic DMD simulations allow 190

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**Fig. 2.** Average RMSD as a function of temperature. Average RMSD is computed using WHAM analysis. Based on the self-consistently determined density of states  $\rho(E)$  and the conditional probability to observe a structure with an RMSD of *R* at the given energy *E*, *P*(*R* | *E*), the average RMSD and corresponding error bar can be computed accordingly (Materials and Methods).

efficient sampling of the large-scale conformational
 dynamics of proteins and protein complexes.<sup>19,30,31</sup>

In order to efficiently sample the conformational 193dynamics of apoSOD1, we utilize replica exchange<sup>32</sup> 194DMD simulations, which allow enhanced sampling 195of the conformational space. We allocate 12 replicas 196 for each SOD1 variant, with each replica running at 197different temperatures from low to high (Materials 198 and Methods). Periodically, replicas with neighbor-199ing temperature values exchange their simulation 200 temperatures stochastically. A temporarily trapped 201202 state in a replica can be rescued by simulating at a 203 higher temperature, thereby enhancing the sam-204 pling efficiency of DMD simulations. For each simulation, we start from the crystal structure 205conformation, with metal ions and the disulfide 206 bond removed. The structures for wild type (Protein 207Data Bank ID: 1SPD) and G37R (Protein Data Bank 208ID: 1AZV) are known. The starting structure of 209 I149T is modeled by amino acid substitution and 210rotamer optimization using Eris.<sup>33</sup> In the simula-211tions, cysteine residues do not form disulfide bond 212 mimicking a reducing condition. The total simula-213tion time of each replica is 100 ns. Therefore, we 214perform a total of 1.2 µs of DMD simulations for 215each SOD1 variant (Materials and Methods). 216

#### 217 ApoSOD1 features frequent local unfolding before 218 global unfolding

Based on replica exchange simulations, we use the weighted histogram analysis method (WHAM; Materials and Methods) to compute the thermodynamics of apoSOD1 unfolding. In WHAM analysis, Unfolding of CU, Zn Superoxide Dismutase Monomer

the density of states is self-consistently determined 223 from overlapping energy histograms for the replica 224 exchange simulations.<sup>34</sup> To reduce structural relax- 225 ation artifacts from the starting crystallography 226 structure, we exclude the first quarter of each 227 simulation trajectory from the WHAM analysis. As 228 a simple approach to test convergence of the 229 simulations, we divide the rest of the simulations 230 into halves, and then compute and compare the 231 histogram of potential energies for each of the half. 232 We find that the histograms from both halves are 233 close to each other, suggesting the convergence of 234 the simulations (Fig. S1). Given the density of states, 235 thermodynamic parameters such as specific heat 236 and average root-mean-square deviation (RMSD) 237 from the starting crystal structure can be calculated 238 (details in Materials and Methods). 239

The specific heat of wild-type apoSOD1 monomer 240 features a major peak at  $T_{\rm f} \sim 330$  K (Fig. 1c), which 241 corresponds to the global unfolding or melting 242 transition of the protein. Above the transition 243 temperature  $T > T_{fr}$  the protein is random coil like 244 with large RMSD (Fig. 2). At lower temperatures, 245 the protein is folded or at least partially folded with 246 lower RMSD. Interestingly, a minor peak appears at 247 a lower temperature,  $T_p \sim 310$  K, which corresponds 248 to a partial unfolding transition. Such a weak 249 structural transition has also been observed in 250 earlier computational studies, although the global 251 unfolding transition was the main focus of these 252 studies, using the melting temperature as the 253 measure of thermal stability.<sup>19</sup> In an earlier work 254 by Zhou and Karplus, a similar transition was 255 termed surface-molten to solid transition.<sup>35</sup> The 256 lower value of the local unfolding temperature as 257 compared to the global unfolding temperature 258 suggests that the apoprotein undergoes significant 259 local unfolding before it becomes globally unfolded 260 (Fig. 2), which is consistent with the NMR study of 261 the wild-type apoSOD1 monomer in solution.<sup>21</sup> 262

We similarly compute the specific heat of the two 263 SOD1 mutants (Fig. 1d). Both mutants have a major 264 and a minor peak in the specific heat, similar to that 265 of the wild type. Because of the vast conformational 266 space of SOD1, we do not expect DMD simulations 267 to reach folding/unfolding equilibrium as observed 268 in simulations of small fast-folding proteins.<sup>27</sup> For 269 example, the melting temperature of wild-type 270 apoSOD1 monomer in DMD simulations (~330 K) 271 is higher than that measured in experiments 272 (~315 K).<sup>36</sup> However, starting from the crystal 273 structure, we expect that our microsecond-long 274 replica exchange simulations would be able to 275 sufficiently sample conformations in the folded 276 and partially folded states (e.g., the convergence of 277 simulations illustrated in Fig. S1 and Fig. 2), and the 278 computed unfolding temperatures can be used as a 279 qualitative measure of a protein's thermostability. 280 Compared to the wild type, the I149T mutant has a 281

lower melting temperature and thus a weaker
thermal stability, while G37R has a similar or
slightly higher melting temperature. Interestingly,
the two mutants have lower local unfolding
temperatures (the low-temperature peak in Fig. 1d)
than that of the wild type, suggesting that mutations
enhance the local unfolding of apoSOD1.

#### 289 Mutations lead to different local unfolding dynamics

In order to characterize the conformational dy-290 namics of different SOD1 variants in the partially 291 unfolded states, we reconstruct the conformational 292ensemble from the replica exchange simulation 293294 trajectories (see Materials and Methods) based on the RMSD ranges identified from WHAM calcula-295tions (Fig. 2). Given the partially unfolded structural 296ensemble for each SOD1 variant, we compute the 297

root-mean-square fluctuation (RMSF) of each resi- 298 due around its average positions (Fig. 3a and c). A 299 larger RMSF value denotes higher conformational 300 flexibility of the residue in the locally unfolded state. 301 We also compute the average RMSD of each residue 302 from the corresponding native structure (Fig. 3b and 303 d). In the RMSD per residue calculation, we exclude 304 the two major loops, residues 51-80 and 121-141, 305 which are coordinated by metal ions in the crystal 306 structure and are highly disordered without metals 307 bound. For the wild type, the three N-terminal 308 strands, the middle strand near residue 100, and the 309 C-terminal strand all feature low RMSD and RMSF 310 values. These results are consistent with previous  ${}^{311}$  experimental  ${}^{22}$  and computational  ${}^{6,19}$  studies of  ${}^{312}$ local unfolding in the apoSOD1 monomer. These 313 same segments were also found to participate in the 314 fibrillar core by wild-type apoSOD1. 315



**Fig. 3.** The local unfolding conformational dynamics of apoSOD1 monomer. The locally unfolded conformational ensemble for each SOD1 variant is reconstructed from the simulation trajectories (Materials and Methods). The corresponding conformational dynamic parameters, including RMSF (a and c) and RMSD (b and d) per residue, are computed based on the reconstructed structural ensemble. In order to estimate the error bars, we split the simulation trajectory into halves and compute the dynamic parameters independently. To avoid overlapping lines, we compare the RMSF and RMSD between WT and G37R (a and c) and between WT and I149T (b and d) separately. The average RMSD per residue is computed with respect to the native states. Due to their large conformational flexibility, we do not include the loops in the RMSD calculation.

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G37R displays larger RMSD and RMSF in the middle strand near residue 100 compared to the wild type, while the N- and C-terminal strands of G37R have low RMSD and RMSF similar to that of the wild type (Fig. 3a and b). In the I149T 320 mutant, the C-terminal strand has larger RMSF 321 and RMSD values than those of the wild type. 322 The N-terminal and middle strands of I149T 323



**Fig. 4.** Thermodynamics of coarse-grained SOD1 monomer: (a) WT, (B) G37R, and (c) I149T. On the left column, the probability of each residue to form the amyloid core ( $P^{Core}$ ) is computed from the experimentally identified, proteolysis-resistant peptides in the amyloid core (Materials and Methods). On the right column, the specific heat of the coarse-grained SOD1 monomer is computed from replica exchange simulations of monomer folding. Due to the experimentally based bias potential, the protein features a stable partially folded intermediate state.

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feature low RMSD and RMSF as is found in the 324 wild type, although the RMSD of the turns in 325I149T is large (Fig. 3c and d). These regions with 326 low RMSD and RMSF values in mutant SOD1 327 correspond to the core-forming peptides in the 328 respective aggregates<sup>7</sup> (Fig. 1). Therefore, there is 329 a correlation between the computationally identi-330 fied stable, native-like regions in the locally 331 unfolded apoSOD1 monomer and the proteoly-332

sis-resistant peptide segments in the correspond- 333 ing amyloid core. Taken together, these results 334 suggest that mutations affect the local unfolding 335 dynamics and result in different patterns of local 336 unfolding. The peptide segments in the well- 337 defined residual structure in the locally unfolded 338 apoSOD1 can serve as a "building block" for fibril 339 aggregates, which interact with each other to form 340 the fibrillar core. 341



**Fig. 5.** The aggregation process of WT SOD1 monomers. (a) The initial configuration of eight SOD1 monomers in the simulation box. The monomer concentration is as high as 1 mM. The cartoon representation is assigned and illustrated by using MOLSCRIPT<sup>40</sup> and PyMOL, respectively. (b) One monomer (indicated by the arrow) associates with the end of the nascent amyloid-like aggregate and forms the cross- $\beta$  core. (c) The associated monomer is incorporated into the aggregate after structural rearrangement. (d) The resulting stable aggregate structure with well-formed cross- $\beta$  core.

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#### 342 Aggregation of apoSOD1 monomers

343 The aggregation of SOD1 is a long timescale process, which takes days, weeks, and months 344under the quiescent condition<sup>37</sup> and hours under 345 the agitated condition.<sup>7</sup> Modeling this process with 346 high-resolution DMD simulations is computational-347 ly challenging. Instead, we use a coarse-grained 348 two-bead protein model in DMD simulations<sup>24</sup> to 349 study the aggregation of apoSOD1 monomers, 350 where a structure-based interaction potential for 351aggregation<sup>24,38</sup> is used (Materials and Methods). To 352 promote the formation of partially unfolded SOD1 353 as observed in both computation and experiments, 354 we assign stronger attractive interactions between 355residues forming the amyloid core. The core-form-356 357 ing residues are identified from proteolysis and mass spectroscopy of the aggregates of SOD1 358 variants (Materials and Methods; Fig. 4). 359

### Experimental constraints promote partial unfolding in SOD1 monomers

We first characterize the coarse-grained monomer 362 folding dynamics of the three SOD1 variants. For 363 each variant, we perform replica exchange DMD 364simulations of the monomer and compute the 365 specific heat using WHAM (Materials and Methods). 366 367 Due to the two types of interactions (structure-based 368 interactions and experimentally derived core in-369 teractions), the coarse-grained SOD1 monomers feature three-state folding dynamics with two 370 distinct peaks in specific heat, which corresponds 371 to folded intermediate and intermediate unfolded 372transitions, respectively<sup>39</sup> (Fig. 4a). Strong attrac-373 tions between the experimentally determined core-374forming residues stabilize the partially unfolded 375intermediates, the structures of which are consistent 376 with the experimentally derived input constraints 377 with the core-forming segments folded (Fig. 4). 378Although the specific heat plots between coarse-379 grained and atomistic simulations of corresponding 380 proteins are different (Fig. 1 and Fig. S1), which is 381 382 expected due to different models and also different types of interaction potentials, they all display two 383 peaks featuring a partially unfolded intermediate. To 384 model the aggregation of SOD1 via the association of 385 the partially unfolded intermediates, we perform 386 equilibrium simulations of multiple SOD1 mono-387

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mers at the average temperature between the two 388 transitions. 389

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#### Formation of amyloid-like SOD1 aggregates

For each SOD1 variant, we perform DMD 391 simulations with eight SOD1 monomers in a cubic 392 box with dimensions of 227 Å, corresponding to a 393 high concentration of approximately 1 mM. At a 394 temperature that promotes local unfolding, each 395 isolated monomer remains in the intermediate state. 396 For example, in wild-type SOD1 monomers, the N- 397 terminal strands (blue strands in Fig. 5a), the central 398 strand 6 (yellow strand in Fig. 5a), and the C- 399 terminal strand (red strand in Fig. 5a) are all folded. 400 The monomers associate with each other in simula- 401 tions and form amyloid-like oligomers (Figs. 5 and 402 6), where the residual strands in each monomer 403 assemble into  $\beta$ -sheets via inter- and intra-monomer 404 hydrogen bonds. These  $\beta$ -sheets face each other to 405 form high-order "cross- $\beta$ " structures as shown by 406 the computed fibrillar diffraction pattern (Fig. 6). 407 There are strands from the same protein incorporat- 408 ed into neighboring sheets, which further stabilize 409 the aggregates in addition to the side-chain-side- 410 chain interactions. Our aggregation simulations of 411 three SOD1 variants demonstrate the formation of 412 amyloid-like aggregates by association of the par- 413 tially unfolded SOD1 monomers. The amyloid-like 414 aggregate structure of SOD1 is not a simple stacking 415 of the residual folded structure but requires a major 416 rearrangement of each monomer. 417

The ends of each fibril core expose unsatisfied 418 hydrogen bond donors and acceptors, which allow 419 for further fibril growth. For instance, in Fig. 5b–d, 420 we illustrate one monomer incorporation event from 421 the wild-type simulation. An SOD1 monomer 422 initially associates with one end of the amyloid- 423 like aggregate by diffusion (Fig. 5b) and undergoes 424 structural rearrangement in order to be incorporated 425 into the ordered aggregate (Fig. 5c and d). In the 426 final aggregate structures, we notice that both wild 427 type (Fig. 5d) and I149T mutant (Fig. 6c) form a 428 single-core aggregate, while G37R forms an aggre- 429 gate with two cores during the course of DMD 430 simulations (Fig. 6b). This result is consistent with 431 the experimentally observed morphology of G37R 432 fibrillar aggregate, which is much thinner, branched, 433 and less ordered compared to the fibrils formed by 434

Fig. 6. The fibrillar aggregates of SOD1: (a) WT, (b) G37R, and (c) I149T. The first and the second columns correspond to the aggregates formed in simulations. Two views are shown by a 90° rotation along the axis of the amyloid fibril. The aggregate of G37R contains two cores. The computed fibril diffraction patterns of the aggregates<sup>24</sup> feature the typical "cross- $\beta$ " characteristics (third column). The peak along the fibril axis corresponds to the hydrogen bonds between strands, and the peak perpendicular to the axis corresponds to the separation between the adjacent  $\beta$ -sheet. The fourth column corresponds to the electron microscopic images of aggregates formed *in vitro*. The SOD1 fibrils were prepared by shaking disulfide-reduced apoSOD1 at 37 °C, 1200 rpm for 50 h (Materials and Methods). A bar in each panel represents 0.1  $\mu$ m.

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wild type and I149T (Fig. 6). Therefore, we postulate that the abundance of flexible loops in partially unfolded G37R results in the formation of many smaller  $\beta$ -rich aggregates and inhibits the formation of the long and discrete fibrillar aggregates observed in wild type and I149T.

In summary, we performed multiscale molecular 441 dynamics simulations describing monomer confor-442 mational dynamics and oligomer formation of 443 apoSOD1 in wild type and two mutants, G37R 444 and I149T, each of which has distinct aggregation 445 morphology and peptide segments forming the 446 fibrillar core. Our simulation results suggested a 447generic SOD1 aggregation mechanism. After the 448 loss of the stabilizing metal ions and disulfide bond, 449 apoSOD1 monomer undergoes significant local 450unfolding before global unfolding. Mutations affect 451the conformational dynamics and result in distinct 452local unfolding patterns. The residual structure of 453the partially unfolded protein exhibits an exposed 454hydrophobic core and unsatisfied hydrogen bond 455donors and acceptors, which is prone to aggregate. 456At aggregation-favoring conditions, including high 457concentration and temperatures that promote local 458unfolding, the partially unfolded apoSOD1 mono-459mers associate into amyloid-like aggregates with 460"cross- $\beta$ " characteristics. The aggregate structure is 461 not formed by a simple stacking of the persistent 462463 residual structure of the monomer but, rather, 464 requires structural rearrangement to form the 465 ordered structure. We also found a correlation between the aggregate structures in simulations 466 and the mesoscopic aggregate morphologies ob-467 served in experiments. Mutant G37R, which forms 468 less ordered fibrillar aggregates in vitro, is found to 469form two smaller amyloid-like cores due to the large 470portion of unstructured segments inhibiting the 471formation of a single ordered "cross- $\beta$ " core as 472 observed in the two other variants (Fig. 5). There-473 fore, mutations affect the residual structure of the 474locally unfolded apoSOD1, where the peptide 475segments serve as the "building block" of SOD1 aggregation.<sup>24,25</sup> The structured and unstructured 476477regions of the partially folded state determine the 478morphology of the aggregates. 479

#### 480 Materials and Methods

#### 481 Atomistic DMD simulations

<sup>482</sup> DMD is a special type of molecular dynamics simulation <sup>483</sup> where pairwise interaction potentials are modeled with <sup>484</sup> discontinuous functions. <sup>41</sup> The algorithm for DMD can be <sup>485</sup> found in Refs. 42 and 43. We use an atomistic DMD force <sup>486</sup> field introduced in Ref. 27 to study apoSOD1 monomer <sup>487</sup> dynamics. Briefly, we use the united-atom model to <sup>488</sup> represent the protein, where all heavy atoms and polar <sup>489</sup> hydrogen atoms are explicitly modeled. The bonded interactions include covalent bonds, bond angles, and 490 dihedrals. We include van der Waals, solvation, and 491 environment-dependent hydrogen bonding interactions in 492 the nonbonded interactions. The solvation energy is 493 modeled using the Lazaridis-Karplus implicit solvation 494 model with the fully solvated conformation as the 495 reference state.<sup>29</sup> The hydrogen bond interaction is 496 modeled using a reaction algorithm.44 In addition to the 497 previous version of the atomistic DMD force field,<sup>27</sup> we 498 also add electrostatic interactions between charged resi- 499 dues, including the basic and acidic residues. We assign 500 integer charges to the central atoms of charged groups: CZ 501 for arginine, NZ for lysine, CG for aspartic acid, and CD for 502 glutamic acid. We use the Debye-Hückel approximation to 503 model the screened charge-charge interactions. The Debye 504 length is set at approximately 10 Å by assuming water 505 relative permittivity of 80 and a monovalent electrolyte 506 concentration of 0.1 mM. We discretize the continuous 507 electrostatic interaction potential with an interaction range 508 of 30 Å, where the screened potential approaches 0 (Fig. 7). 509 We use the constant volume DMD simulations with period 510 boundary conditions and control the simulation temper- 511 ature using the Anderson thermostat.<sup>45</sup> 512

#### Replica exchange simulations and WHAM analysis 513

We use the replica exchange method to perform 514 simulations of multiple copies of the same system in 515 parallel at various temperatures. At given time intervals, 516 replicas with neighboring temperatures exchange temper-517 ature values according to a Metropolis-based stochastic 518 algorithm. We set the temperature exchange interval as 519 50 ps. Exchange between replicas increases the sampling 520 efficiency in that energetic barriers can be overcome more 521 easily and, in less time, with exposure to higher 522



Fig. 7. Screened Debye–Hückel potential function between two opposite single charges. The continuous potential has a Debye length of  $\sim 10$  Å, assuming the relative permittivity of water of 80 and a monovalent salt concentration of 0.1 mM. The step function in red is the discretized step function utilized in DMD simulations. For two atoms of the same charge, we change the sign of the potential to indicate a repulsive.

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temperatures. In our simulations, we allocate 12 replicas with temperatures of 270, 282, 294, 303, 312, 321, 330, 339, 345, 352.5, 365, and 377.5 K for the simulations of apoSOD1 monomers.

We perform WHAM analysis using the trajectories from the replica exchange simulations. The WHAM method 528utilizes multiple simulation trajectories with overlapping 529530sampling along the reaction coordinates to self-consistently compute the density of states  $\rho(E)$  by combining histograms from different simulation trajectories.<sup>34</sup> Given the density of 531532states, the folding specific heat  $(C_v)$  can be computed at 533534various temperatures according to the partition function  $Z = \int \rho(E) exp(-E/k_B T) dE$ . Here,  $k_B$  is the Boltzmann 535 constant. To compute the average RMSD as a function of 536 537 temperature, we compute the conditional probability P(A | E)by observing a structure with an RMSD of A at the given 538 539 energy E, evaluated from all simulation trajectories. The average RMSD as a function of temperature can be computed 540 as  $\langle A(T) \rangle = 1 / Z \int A \cdot P(A | E) \rho(E) exp(-E / k_B T) dE dA$ . We 541 also estimate the error bars as statistical uncertainty<sup>46</sup> in the 542 WHAM estimation of specific heat and average RMSD. The 543 temporal correlation in sequentially generated configurations 544 is obtained by autocorrelation analysis. 545

#### 546 **Reconstruction of the locally unfolded states**

We use an RMSD range  $[D_{\min}, D_{\max}]$  to identify the 547locally unfolded structures from the trajectories. In order to 548identify the cutoff values, we compute average RMSD as a 549function of temperature using WHAM analysis (Fig. 2). 550From the specific heat, we identify the transition temper-551552ature at low temperatures corresponding to local unfolding,  $T_1$ . We assign the average RMSD at  $T_1$  as  $D_{min}$  for each 553of the three SOD1 variants. For all three SOD1 variants, the 554melting or global unfolding starts from a state with an 555average RMSD of approximately 10 Å (Fig. 2). Therefore, 556we use a  $D_{\text{max}}$  of 10 Å for all three variants. 557

#### 558 Coarse-grained DMD simulations

We use a two-bead protein model to study apoSOD1 aggregation.<sup>24,47</sup> In the two-bead model, each amino acid 559560is represented by only the  $\alpha$ -carbon (backbone) and  $\beta$ -561carbon (side chain). The bonded interactions between 562563neighboring atoms along the peptide chain are assigned so as to mimic peptide geometry.<sup>47</sup> We use a structure-based 564potential to model the side-chain-side-chain packing 565interactions, where native interactions in the native state 566 as observed in the crystal structure are favored. Two 567interacting residues can form either intra- or inter-568569monomer contacts, in order to promote protein-protein association.<sup>24,38</sup> The attractions between  $\beta$ -carbons are 570assigned with a hardcore distance of 3 Å and an 571interaction range of 7.5 Å. We also model the backbone-572backbone hydrogen bond interaction as in Ref. 24. 573

To stabilize the partially unfolded state, where the 574575amyloid-core-forming residues remain folded, we assign a strong attraction between the core residues. In the 576proteolysis/mass spectroscopy study of aggregates, 577 578there are overlapping peptides observed for each coreforming region (e.g., the N-terminal region for wild-type 579SOD1).<sup>7</sup> For all of the *overlapping peptides* observed 580experimentally, we assume that each peptide has an 581

equal chance to participate in the amyloid core. Therefore, 582 we can compute the probability for each residue in a given 583 region to be observed in the amyloid core,  $P^{\text{Core}}(i)$  (Fig. 4). 584 By combing all regions, we obtain the core-forming 585 probability for all residues. We therefore introduce an 586 experimentally derived bias potential to the structure- 587 based potential: 588

$$E_{ij} = \left[\varepsilon^{G^{-}o} + \left(\varepsilon^{Core} - \varepsilon^{G^{-}o}\right)P^{Core}(i)P^{Core}(j)\right]\Delta_{ij}$$

Here,  $\Delta_{ij}$  is the native interaction matrix, which equals 1 if 599 the two residues *i* and *j* are in contact in the native state 592 and 0 otherwise.  $\varepsilon^{G\delta}$  and  $\varepsilon^{\text{Core}}$  are the energy scales for the 593 structure-based and experimentally determined bias 594 potentials, correspondingly. In our simulations, we assign 595  $\varepsilon^{G\delta} = 0.5 \varepsilon_0$  and  $\varepsilon^{\text{Core}} = 1.0 \varepsilon_0$  with  $\varepsilon_0$  as the energy unit. The 596 hydrogen bond interaction strength is 2.0  $\varepsilon_0$ .

### Electron microscopic observation of *in vitro* SOD1 fibrils

Preparation and observation of SOD1 fibrils (WT, G37R, 600 and I149T) were performed as described previously.<sup>7</sup> 601 Briefly, following constant agitation of 100 mM SOD1 at 602 37 °C, 1200 rpm for 50 h, we collected insoluble aggregates 603 by ultracentrifugation at 110,000g for 30 min. In order to 604 avoid shearing fibrillar structures during agitation, we 605 further performed a seeding reaction by adding 10 mM 606 SOD1 aggregates (monomer based) to 100 mM soluble 607 SOD1 and incubating the mixture at 37 °C for 3 days in the 608 absence of agitation. Insoluble pellets were again collected 609 by ultracentrifugation, resuspended in pure water, and 610 adsorbed on 400-mesh grids coated by a glow-charged 611 supporting membrane. After negative staining with 1% 612 uranyl acetate, images were obtained using an electron 613 microscope (1200EX, JEOL). 614

Supplementary materials related to this article can be 615 found online at doi:10.1016/j.jmb.2011.12.029

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